## 2021 Soil Mechanics I and Exercises Midterm Exam

2021/11/30 (Tue.) Test time 13:15-14:15, Submission due by 14:30 on PandA

## Attention:

- The exam consists of two questions. Separate answer sheet for each major question. Write your name and the question number **on ALL pages**. You may answer a major question over multiple answer sheets, but do not answer multiple major questions on the same answer sheet.
- If possible, combine all answer sheets in sequence and submit as a single file. When submitting multiple files for multiple answer sheets, please order them and set the file names in a way that the question number as well as the page number of answer sheet is understandable.
- Wherever necessary, specify the units in your answers.
- Stop writing the answer at 14:15 and submit the answer sheet via PandA by 14:30. Only when you cannot submit via PandA due to network troubles, etc., submission by email to <u>takai.atsushi.2s@kyoto-u.ac.jp</u> can be accepted.
- Your submission will not be accepted after the deadline for any reason. Give yourself ample time to get through PandA for submitting the answer sheets.
- During the examination, you may consult the lecture materials and reference sources, but consultation with others is strictly prohibited.
- Answer sharing and copying is academic dishonest. Close similarity in answers will result in failed credit of the course and serious penalties.

## [Question 1]

1) Answer the following questions. Graphics may be used if necessary.

- (1) Explain the reason briefly why soils with higher clay content generally have larger plastic index in spite of having the same mineral compositions.
- (2) In general, while clay deposit has comparatively higher void ratio than sand deposit, clay deposit exhibits smaller coefficient of permeability. Explain the reason of this phenomena briefly.
- (3) Explain the definitions of void ratio and porosity briefly, and formulate the relationship between those two parameters.
- 2) Answer the following questions regarding the ground profile shown in Figure 1. Assume the density of water  $\rho_w = 1.00 \text{ Mg/m}^3$  (= 1.00 g/cm<sup>3</sup>) and the gravitational acceleration  $g = 9.80 \text{ m/s}^2$ .
  - (1) Determine the degree of saturation above the groundwater level. Note that the void ratios above and below the groundwater level are the same.
  - (2) The maximum and the minimum dry densities of the sand layer are 1.68 Mg/m<sup>3</sup> and 1.34 Mg/m<sup>3</sup>, respectively. Determine the relative density of the sand layer. Maximum and minimum dry densities correspond to dry density with minimum and maximum void ratios, respectively.

- (3) The embankment was constructed to achieve a water content of 15.0% and a dry density of 1.60 Mg/m<sup>3</sup>, using soil having a water content of 10.0% at an excavation site. Calculate the mass of soil collected at the excavation site necessary for a a unit site area (1.00 m<sup>2</sup>) of the embankment.
- (4) Determine the total stress, the pore water pressure and the effective stress at the bottom of the sand layer.



Figure 1

## [Question 2]

Consider the steady-state flow through an isotropic and homogeneous permeable layer on a horizontal impermeable layer. Herein,  $h_1$  and  $h_2$  represent the total heads of two known points and k is the permeability coefficient of the permeable layer. Assume that the Darcy's law can be applied and the hydraulic gradient i in the horizontal direction is equal to the slope of the piezometric surface and is an invariant with depth z, complete the following questions.

- 1) When the two-dimensional seepage (uniform in the width direction) of Fig. 2 is considered as the plane of horizontal flow whose constant boundary conditions are  $x = x_1$ ,  $h = h_1$  and  $x = x_2$ ,  $h = h_2$ , answer the questions below.
  - (1) Express the discharge velocity *u* in the *x* direction in terms of differential form of the piezometric head *h*.
  - (2) In regard to (1), express the flow rate q per unit width of the plane through any vertical section.
  - (3) As q is constant along any distance x between  $x_1$  and  $x_2$ , express k from (2), after integration and substitution of the boundary conditions.
  - (4) Determine the piezometric head *h* at a distance *x* in terms of *x*,  $x_1$ ,  $x_2$ ,  $h_1$ , and  $h_2$ .





- 2) When the radial seepage at any radius *r* from the center of a pumping well is considered as the plane of axisymmetric flow whose constant boundary conditions are  $r = r_1$ ,  $h = h_1$  and  $r = r_2$ ,  $h = h_2$ , answer the questions below. Note that  $r_w$  is a radius of the pumping well and  $h_w$  is a water level in the pumping well.
  - (1) Express the volume flow rate q in an unconfined permeable layer through any vertical section of Fig. 3, in terms of difference form of the piezometric head h, using parameters given in the figure.
  - (2) As q is constant along any radius  $r \geq r_w$ , express k from (1), after integration and substitution of the boundary conditions.





(3) If the permeable layer with a thickness of H is confined by upper and lower impermeable layers, express the volume flow rate q in a confined permeable layer through any vertical section of Fig. 4.

(4) As q is constant along any radius  $r \geq r_w$ , express k from (3), after integration and substitution of the boundary conditions.



Figure 4

- (5) A pumping well with a radius  $r_w$  of 0.100 m was installed in an unconfined permeable layer as shown in Fig. 3. The water levels measured from two observation wells were  $h_1 = 105$  m at  $r_1 = 10.0$  m and  $h_2 = 125$  m at  $r_2 = 100$  m. Once the pumping well reached a steady state, calculate the water level  $h_w$  in the pumping well.
- (6) When the pumping test was conducted under the same conditions as (5) in a permeable layer with a thickness H = 40.0 m, confined between two impermeable layers as shown in Fig. 4, the same water level as (5) was obtained for each observation well. Calculate the water level  $h_w$  in the pumping well.